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**Discussion on Influence Factors of High Speed Train Running Safety
on Bridge during Earthquake**

Lizhong Jiang¹⁾, Xiang Liu²⁾

1), 2) School of Civil Engineering, Central South University, Changsha 410075, China

2) liuxiang2017@csu.edu.cn

Abstract

The bridge structure occupies a high proportion in the high-speed railway (HSR) line. When the earthquake occurs, the probability of train running on the bridge is high. The large amplitude vibration of track bridge structure will endanger the train running safety (RS). In order to discuss the influence factors of HSR RS on bridge under earthquake action, the coupling vibration model of train track bridge is established, and the influence of structural natural vibration period, train running speed and track irregularity on RS of HSR train on bridge during earthquake is discussed respectively. The results show that the natural vibration period of the structure has a great impact on the train RS, and different ground motion samples show different results; generally, the derailment coefficient of the train increases with the increase of the vehicle speed; the track irregularity has a certain impact on the train RS.

1. INTRODUCTION

China is located between the circum Pacific seismic zone and the Eurasian seismic zone, which is the two major seismic zones in the world. It is squeezed by the Pacific plate, India plate and Philippine Sea plate. The seismic fault zone is very active, and more than half of the high-speed railway (HSR) lines are in the earthquake area (Feng 2019; Jiang 2019a; Zhang 2020; Yu 2020). For example, the Beijing-Shanghai HSR crosses four major seismic zones. With the operation of HSR more frequent, and the

1) Professor.

2) Graduate student.

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bridge line occupation ratio is large, so when the earthquake occurs, there is a greater probability that there will be a train running on the bridge. The large amplitude vibration of bridge structure under earthquake will seriously affect the running safety (RS) of train, and once the train derails or overturns at high speed, it will cause great impact.

In terms of scientific research, there have been rich achievements in the safety of trains on bridges under earthquake. For example, (Zeng 2015), (Xu 2017), (Zhang 2010) studied the response of vehicle bridge coupling system and RS from the perspective of random vibration; the linear complementarity problem (LCP) was used to analyze the nonlinear vehicle bridge vibration and RS under earthquake by (Zeng 2018); (Du 2012) discussed the non-uniform excitation input of long-span bridge under earthquake; (Jin 2016) discussed the influence of vertical earthquake on train RS on bridge. (Tanabe 2008), (Nishimura 2015) summarized the derailment mechanism of trains through shaking table test and numerical simulation. Due to the excessive literature, we will not list them here. (Luo 2007) put forward a simple train RS calculation theory, and introduced that the maximum speed PV and speed spectral density Sf on the rail surface are used as train design indexes to consider train RS.

2. Train-Track-Bridge Coupled Model

2.1. Model of train.

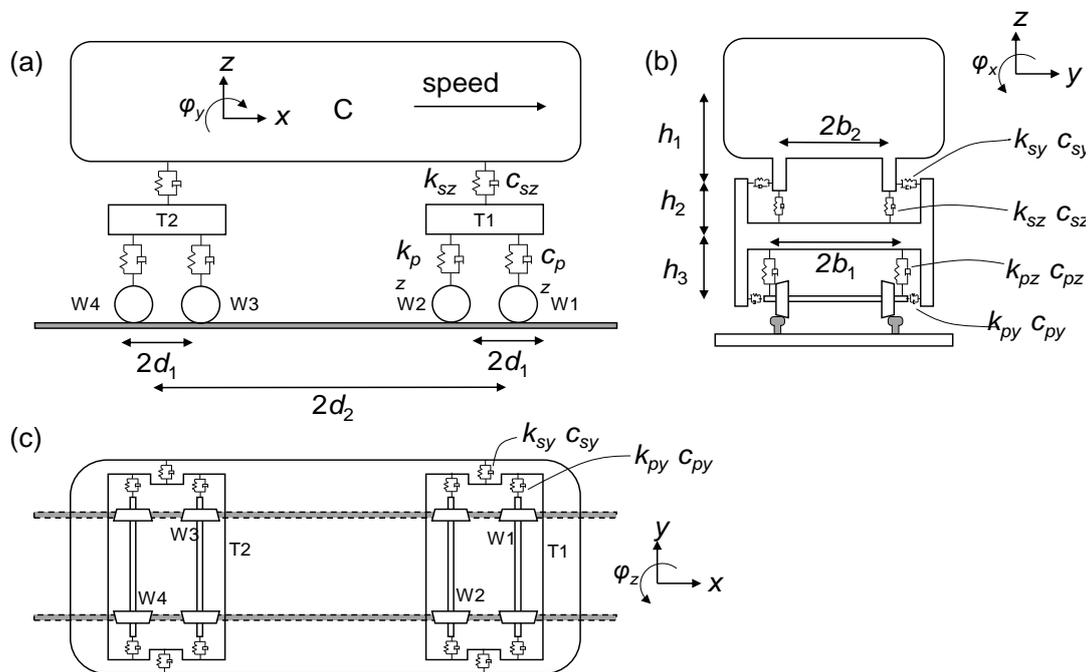


Fig. 1 model of train.

The schematic diagram of HSR train model is shown in Fig. 1. Each carriage contains one car-body, two bogies and four wheel sets. The train is simulated by mass-

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spring-damping system, in which the body, bogie and wheelset are all rigid bodies. The secondary suspension between car-body and bogie and the primary suspension between bogie and wheelset are simulated by spring-damping system.

Five independent degrees of freedom (DOF) including lateral, vertical, roll, pitch and yaw are considered for both vehicle and structure, and 4 independent degrees of freedom are considered for wheelset. Therefore, the whole carriage includes 31 independent DOFs, as shown in Table 1. The train coordinate system adopts the right-hand coordinate system.

Table 1 Train corresponding degree of freedom.

	lateral	vertical	roll	pitch	yaw
Car-body	y_c	z_c	φ_c^x	φ_c^y	φ_c^z
Front bogie	y_{T1}	z_{T1}	φ_{T1}^x	φ_{T1}^y	φ_{T1}^z
Rear bogie	y_{T2}	z_{T2}	φ_{T2}^x	φ_{T2}^y	φ_{T2}^z
First wheelset	y_{W1}	z_{W1}	φ_{W1}^x	-	φ_{W1}^z
Second wheelset	y_{W2}	z_{W2}	φ_{W2}^x	-	φ_{W2}^z
Third wheelset	y_{W3}	z_{W3}	φ_{W3}^x	-	φ_{W3}^z
Fourth wheelset	y_{W4}	z_{W4}	φ_{W4}^x	-	φ_{W4}^z

2.2. Train displacement vector.

Taking a single train as an example, the displacement vector of the train can be expressed as,

$$\mathbf{X}^{Vi} = [\mathbf{X}_c^{Vi} \quad \mathbf{X}_{T1}^{Vi} \quad \mathbf{X}_{T2}^{Vi} \quad \mathbf{X}_{W1}^{Vi} \quad \mathbf{X}_{W2}^{Vi} \quad \mathbf{X}_{W3}^{Vi} \quad \mathbf{X}_{W4}^{Vi}]^T \quad (1)$$

with $\mathbf{X}_c^{Vi} = [y_c \quad z_c \quad \varphi_c^x \quad \varphi_c^y \quad \varphi_c^z]^T$; $\mathbf{X}_{Tj}^{Vi} = [y_{Tj} \quad z_{Tj} \quad \varphi_{Tj}^x \quad \varphi_{Tj}^y \quad \varphi_{Tj}^z]^T, j=1, 2$;

$\mathbf{X}_{Wj}^{Vi} = [y_{Wj} \quad z_{Wj} \quad \varphi_{Wj}^x \quad \varphi_{Wj}^z]^T, j=1, 2, 3, 4$.

2.3. Train dynamics equation

The principle of elastic potential energy invariability and the principle of "taking the right seat" (Zeng 1999) can quickly obtain the dynamic equation of the time-varying system of train-track-bridge. In this paper, the mass, stiffness and damping matrices of the train are obtained by this theory. The dynamic equation of the train is

$$\mathbf{M}^V \ddot{\mathbf{X}}^V + \mathbf{C}^V \dot{\mathbf{X}}^V + \mathbf{K}^V \mathbf{X}^V = \mathbf{F}^V \quad (2)$$

where \mathbf{M}^V , \mathbf{C}^V and \mathbf{K}^V are the mass, damping and stiffness matrix of train, respectively; \mathbf{X}^V , $\dot{\mathbf{X}}^V$ and $\ddot{\mathbf{X}}^V$ are the displacement, velocity and acceleration vector of

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train, respectively; The load vector \mathbf{F}^v includes the gravity of the train itself, the force generated by seismic acceleration and the force generated by wheel rail contact. The wheel-rail force is more complex and will be described in section 2.4.

2.4. Wheel-rail contact.

The normal force and creep force of wheel-rail are produced by wheel rail contact. The train and track bridge structure are coupled into a large system through the wheel rail relationship. In this paper, the wheel-rail contact is assumed to be knife-edge contact constraints (Cheng 2017; Zeng 2018), that is, the ideal conical tread, and the rail is regarded as a hinge point. As shown in Fig. 2, the lateral clearance between wheel and rail is 10 mm, and the lateral contact stiffness k_{ry} is $1.617 \times 10^7 \text{N/m}$ (Cheng 2017).

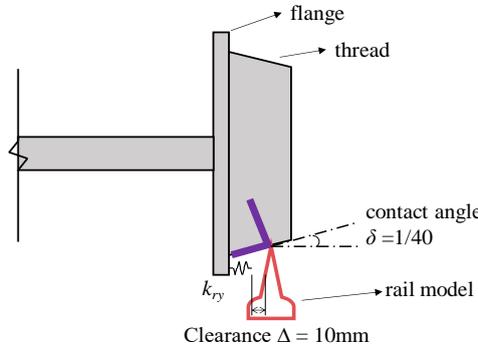


Fig. 2 Wheel-rail contact.

The wheel rail vertical force is calculated by Hertz contact theory, which can be expressed as

$$P_{hz} = G^{-1.5} \Delta_{wr}^{1.5} \quad (3)$$

where G is the constant; Δ_{wr} is the wheel-rail relative compression, and according to the displacement relationship, the compression of Hertz spring can be obtained by simplified calculation,

$$\begin{cases} \Delta_{wr,i}^L = -(z_{wi} + b_w \varphi_{wi}^x - z_{Ri}^L), & \text{if } \Delta_{wr,i}^L < 0, \Delta_{wr,i}^L = 0 \\ \Delta_{wr,i}^R = -(z_{wi} - b_w \varphi_{wi}^x - z_{Ri}^R), & \text{if } \Delta_{wr,i}^R < 0, \Delta_{wr,i}^R = 0 \end{cases} \quad (4)$$

where the subscript i represents the i^{th} wheelset and the corresponding rail position; the superscript R and L represent the right and left rail respectively; z_{Ri}^L and z_{Ri}^R are the vertical displacement of the left and right rail respectively.

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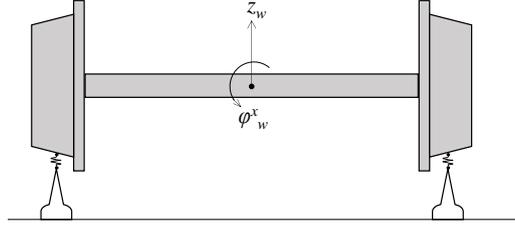


Fig. 3 Calculation of wheel-rail contact geometric state.

Kalker linear creep force model (Kalker 1967) is adopted for the creep force, and Shen–Hedrick–Euristic (Shen 1983) nonlinear creep model is used for large creep.

2.5. Track-bridge model of HSR.

In this paper, the finite element method (FEM) is used to establish the track-bridge system. The spatial Euler-Bernoulli beam element is used to simulate the rail, track slab, bridge and pier. The fastener between rail and track plate is connected by discrete spring damping. The bearing between the main beam and the pier is connected by spring damping. The bottom of the pier is connected with the earth by spring damping. As the main research object of this paper is bridge structure, in order to reduce the degree of freedom, the subgrade section is assumed to be rail rigid subgrade. The damping of bridge structure is relatively complex, and the comprehensive effect of structural damping can be simulated by proportional damping (Liu 2020a), which is simplified as the proportional combination of mass and stiffness

$$\mathbf{C}^b = \alpha \mathbf{M}^b + \beta \mathbf{K}^b \quad (5)$$

where \mathbf{M}^B and \mathbf{K}^B are mass and stiffness matrix of structures. For common Rayleigh damping, there are:

$$\begin{cases} \alpha = 2\omega_1\omega_2 \frac{\xi_2\omega_1 - \xi_1\omega_2}{\omega_1^2 - \omega_2^2} \\ \beta = 2 \frac{\xi_1\omega_1 - \xi_2\omega_2}{\omega_1^2 - \omega_2^2} \end{cases} \quad (6)$$

where ω_1 and ω_2 are the first and second order natural frequencies of structures; ξ_1 and ξ_2 are the damping ratio of the first two modes.

The stiffness, mass and damping matrices are assembled by the FEM to obtain the overall stiffness, mass and damping matrices. Then, according to the structural dynamics, the dynamic equation of the bridge is obtained as follows

$$\mathbf{M}^B \ddot{\mathbf{X}}^B + \mathbf{C}^B \dot{\mathbf{X}}^B + \mathbf{K}^B \mathbf{X}^B = \mathbf{F}^B \quad (7)$$

where \mathbf{X}^B is the displacement vector of the bridge; \mathbf{F}^B is the load vector of the bridge, including the wheel rail force caused by wheel rail contact and the inertial force generated by seismic excitation.

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2.6 Dynamic equation of the system.

By combining Eqs.(2) and (7), the dynamic equation of the system can be obtained as follows

$$\begin{cases} \mathbf{M}^V \ddot{\mathbf{X}}^V + \mathbf{C}^V \dot{\mathbf{X}}^V + \mathbf{K}^V \mathbf{X}^V = \mathbf{F}^V \\ \mathbf{M}^B \ddot{\mathbf{X}}^B + \mathbf{C}^B \dot{\mathbf{X}}^B + \mathbf{K}^B \mathbf{X}^B = \mathbf{F}^B \end{cases} \quad (8)$$

In this paper, Wilson- θ is used for iterative calculation.

3. INFLUENCE FACTOR.

3.1. Influence of bridge natural vibration period on train operation.

For the same seismic wave input, the dynamic response of bridge structure will change with the natural vibration characteristics of the bridge, and the change of rail response will directly affect the RS of train. In order to discuss the influence of different bridge structure natural vibration period on train RS, under the same speed (300km/h), by changing the bridge height to change the natural vibration period of bridge structure, a total of 10 kinds of pier height are calculated. The minimum value of the first transverse period is 0.104 s, and the maximum value is 1.582 s. Five ground motion (GM) samples (Kobe wave, Loma Prieta wave, Northridge wave, Tabas Iran wave and Trinidad wave (2019)) are input into the train-track-bridge system, and the maximum ground acceleration is 0.3g. The same set of samples generated from the track power spectral density function (PSD) of China's HSR are used. The maximum values of train derailment coefficient (Q/P) under different GM samples and different bridge transverse first period are shown in Fig. 4. It can be found that, except for Trinidad wave, the maximum value of train Q/P under other GM sample conditions will change obviously with the change of bridge period, and the overall trend is that the Q/P increases with the increase of the period. In addition, it can be found that the results obtained by different GM samples are quite discrete.

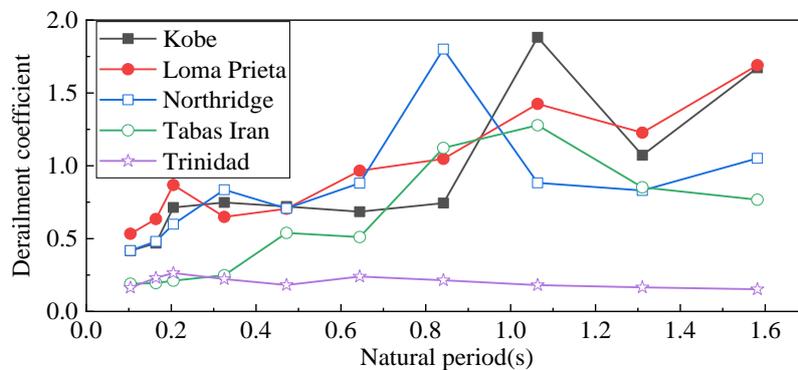


Fig. 4 Maximum value of Q/P under different structural periods.

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3.2. Influence of train speed on train running safety.

When the train speed increases, the excitation of track irregularity is more frequent, and the creep force of wheel-rail will change with the speed, which will affect the RS of the train (Liu 2020b). The results of references (Xia 2006; Xiao 2012; Ju 2012) showed that train speed has a certain impact on the RS of HSR trains under earthquake. In order to explore the influence of vehicle speed on the RS of HSR trains on the bridge, five GM samples (consistent with section 3.1) are also selected, and the maximum ground acceleration is 0.3g. The first lateral period of the bridge is 0.3244s. The same set of samples generated from the PSD of China's HSR are used. The maximum values of Q/P corresponding to different GM samples at different speeds are obtained as shown in Fig. 5. It can be found that the maximum Q/P of the other three waves increases with the increase of vehicle speed except Tabas Iran wave and Trinidad wave.

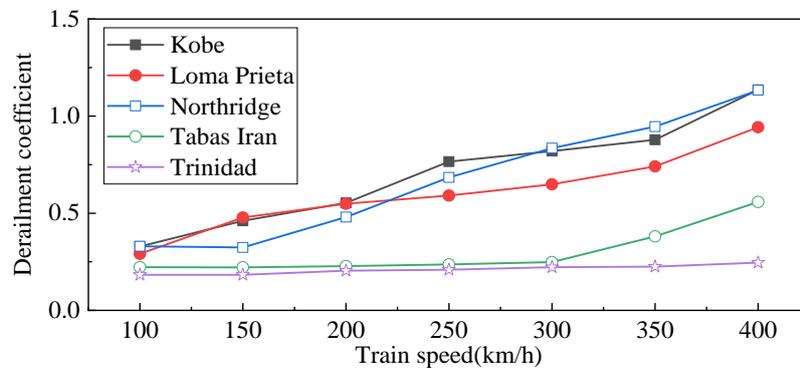


Fig. 5 Maximum value of Q/P under different train speeds.

3.3. Influence of track irregularity on train RS.

Track irregularity is applied to the train-track-bridge system as an incentive, which will affect the stability of the train and the RS of the train (Jiang 2019b). In order to discuss the influence of track irregularity on train RS on bridge during earthquake, two models are established, one is considering track irregularity and the other is not considering track irregularity. Three original GM samples of Kobe wave, Northridge wave and Loma Prieta wave are used. In each case, the same irregularity sample is used. The time-history curves of Q/P under two working conditions when the train running speed is 300km/h are shown in Fig. 6. It can be seen that the Q/P in the case of no track irregularity is basically unchanged, and the Q/P with track irregularity has a small amplitude oscillation before the input seismic wave. After the input of seismic waves, the Q/Ps of the two conditions change greatly, and the trend is relatively consistent. The Q/Ps of the three GM samples with irregularities are greater than those without irregularities.

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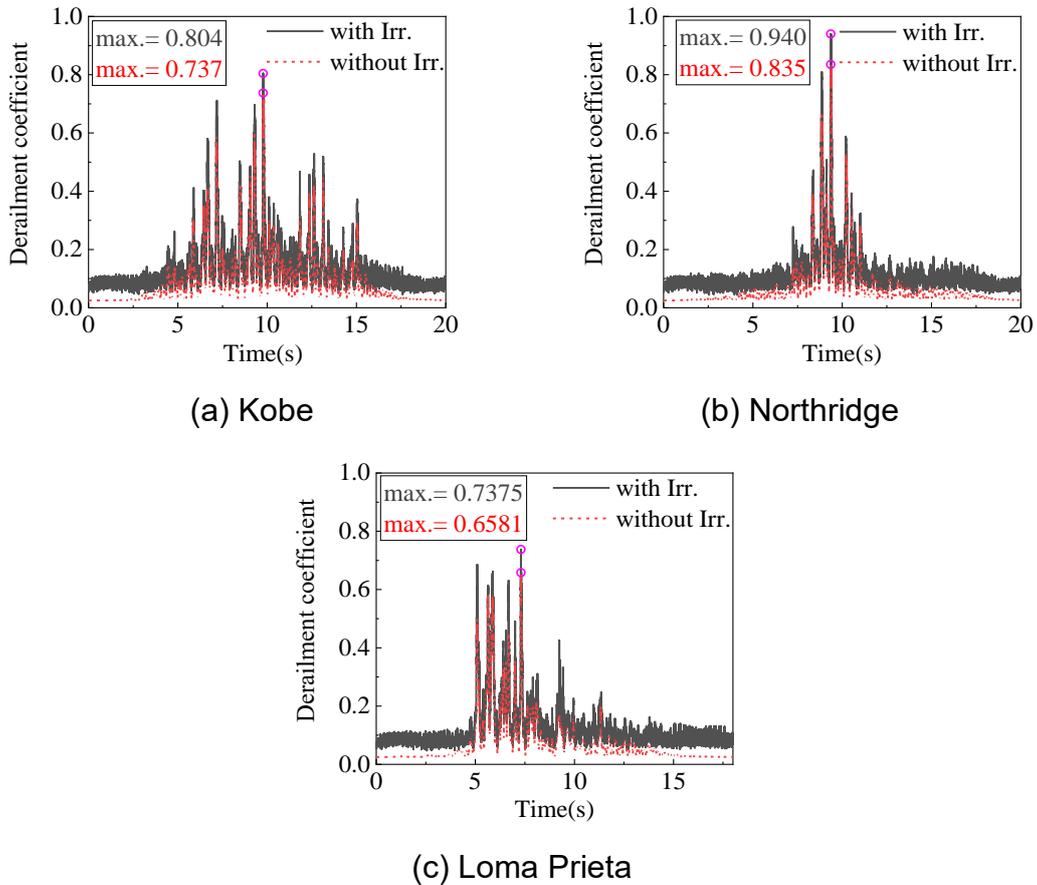


Fig. 6 Time history response of Q/P with and without irregularity.

Fig. 7 shows the maximum values of Q/P under different speed conditions with and without irregularities. Generally speaking, with and without irregularities, the Q/P will increase with the increase of vehicle speed, but the increase range of different GM samples is different; in addition, the Q/P of irregularity condition is greater than that of no irregularity condition.

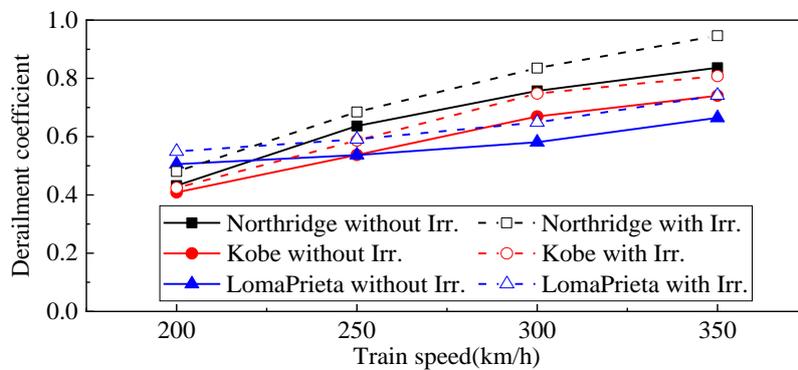


Fig. 7 The maximum values of Q/P corresponding to different speeds with and without irregularities.

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4. CONCLUSIONS

In order to discuss the influence factor on train running safety on the bridges during earthquake, the dynamic model of train-track-bridge coupled model is established, and FEM theory is applied to simulate track-bridge system; mass-spring-dashpot systems are used to simulate the train; the knife-edge contact constraints are used to deal with wheel-rail contact. The influences of natural vibration period of bridge, train speed and track irregularity on the running safety of train are discussed. The results are as follows:

- (1) The natural vibration period of the structure has a great impact on the train RS, and different ground motion samples show different results;
- (2) The derailment coefficient of the train increases with the increase of the vehicle speed;
- (3) The track irregularity has a certain impact on the train RS.

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